

# Safety, Liquidity, and the Natural Rate of Interest

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## Comment 1: Decomposing long term yield into expectation and term premium

This is one core question in the term structure literature

$$y_t^n = \bar{y}_t^n + tp_t^n$$

where

$$\bar{y}_t^n = \frac{1}{n} E_t [r_t + r_{t+1} + \dots + r_{t+n-1}]$$

Expectation  $\bar{y}_t^n$  is the trend.

## Comment 1: Expectation

The short rate

$$r_t = \delta_0 + \delta_1' X_t$$

Dynamics for factors

$$X_{t+1} = \mu + \rho X_t + \Sigma \varepsilon_{t+1}, \quad \varepsilon_{t+1} \sim N(0, I)$$

Pricing equation

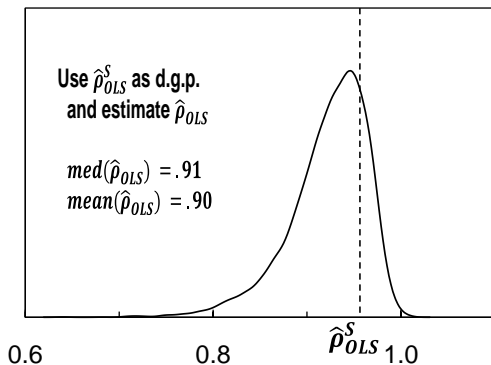
$$P_{nt} = \mathbb{E}_t[\exp(-m_{t+1}) P_{n-1,t+1}]$$
$$y_{nt} = -\frac{1}{n} \log(P_{nt})$$

Expectations

$$E_t[r_{t+n}] = \delta_0 + \delta_1' E_t[X_{t+n}]$$

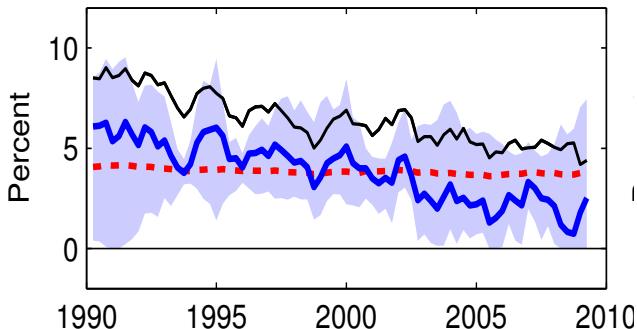
## Comment 1: Bias correction

- ▶ Estimation: OLS for VAR. Highest eigenvalue of  $\rho$ : 0.95.
- ▶ However, the persistence is underestimated.



- ▶ Bias correction: Bauer, Rudebusch, and Wu (2012, 2014).

## Comment 1: Downward trend in expectation

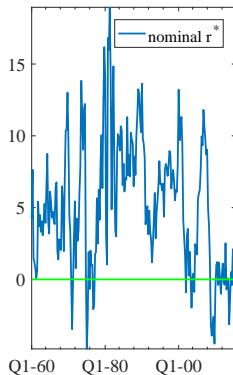
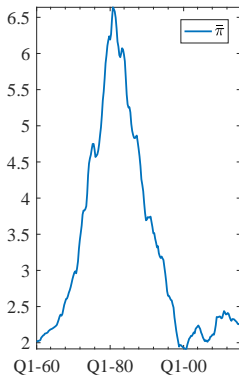
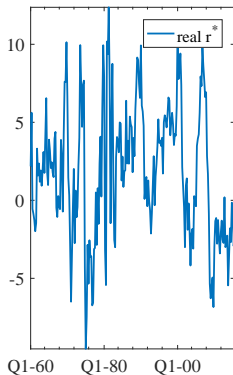


black: five-by-five-year forward rate

Red: OLS

blue: Bauer, Rudebusch, and Wu (2012, 2014) bias corrected

## Comment 2: How negative can nominal rates be?



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Nominal  $r^*$  was as negative as -5%.

Is it plausible?

- ▶ We do not observe negative interest rates in the US.
- ▶ The SNB's deposit rate is at record low of -75 basis points. But that's still far away from -5%.
- ▶ The negative interest rates in Europe were due to interventions by central banks, but  $r^*$  is in the counterfactual world where there is no central bank.

Frictions that potentially allow a negative nominal rate

- ▶ take physical currency out of circulation
  - ▶ highly unlikely
- ▶ storage cost
  - ▶ there is a limit

## Comment 2: What causes implausibly negative nominal rate?

### Lack of proper treatment for ZLB

- ▶ In the reduced form: discard short rate after 2008 Q3

### Consequences

- ▶ internal inconsistency
  - ▶ remove short rate and its ZLB
  - ▶ forward looking agents factor the ZLB in the future into yields at longer maturities.
  - ▶ the same lower bound should constrain the nominal trend and  $r^*$ .
- ▶ less information leads to less accurate estimation



## Comment 2: Shadow rate – a treatment for ZLB

Black (1995)

$$r_t = \max(s_t, \underline{r}),$$

- ▶ Allow the model to be internally consistent
  - ▶ short rate, trend on nominal rates, and expectations in longer rates are subject to the same lower bound.
- ▶ Does not allow nominal rates to be (too) negative.

## Comment 2: Shadow rate – a treatment for ZLB

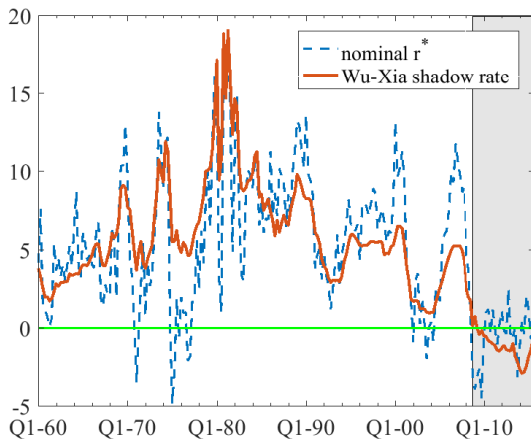
Wu and Zhang (2016)

- ▶ DSGE linear in  $s_t$
- ▶  $r_t = \max(s_t, \underline{r})$
- ▶ A negative  $s_t$  accommodates unconventional monetary policy

Potential consolidating negative nominal rates by relabeling  $r_t$  as  $s_t$

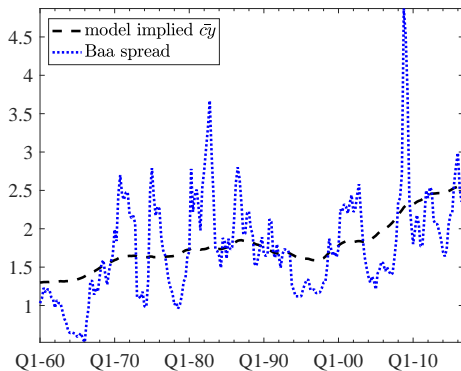
- ▶  $s^* + E_t \pi_{t+1} < 0$
- ▶  $r^* + E_t \pi_{t+1} > 0$
- ▶ A downward trend in  $s^*$  instead of  $r^*$  at the ZLB.

## Comment 2: Shadow rate – a treatment for ZLB



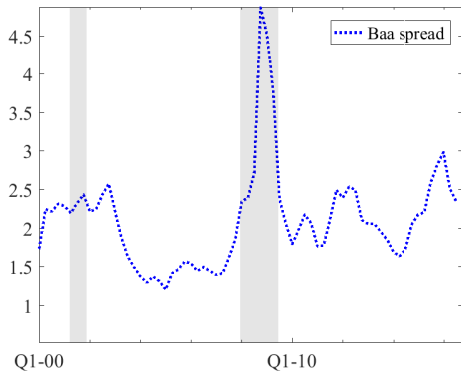
Puzzle remaining: what happened in the 1970s?

## Comment 3: Trend in convenience yield



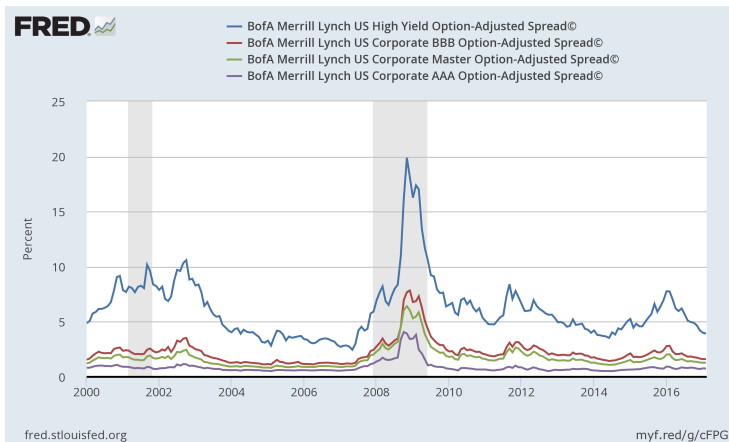
Main result: a trend in convenience yield from late 1990s explains the decline in  $\bar{r}$ .

## Comment 3: No trend in the data



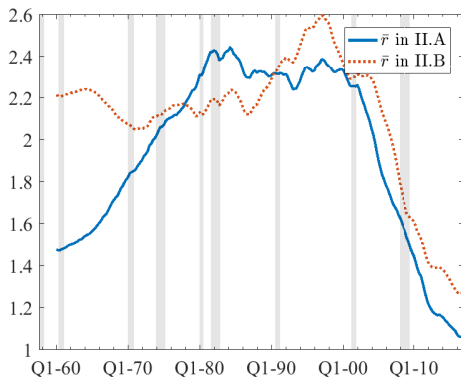
- ▶ No trend is present in the data
- ▶ Spread jumps up during the Great Recession

## Comment 3: No trend in the data



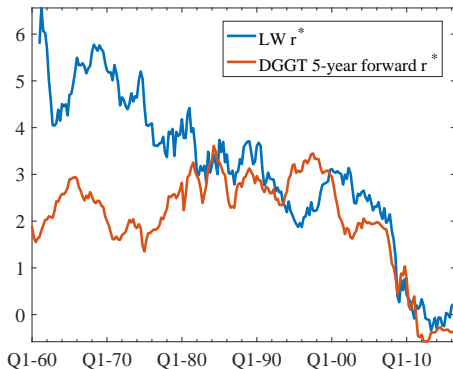
- ▶ No trend is present in the data
- ▶ Spreads jump up during the Great Recession

## Comment 4: Model dependent results



- ▶ For the first 70% of the sample, the correlation is 0.37
- ▶ The difference was 0.8% at the beginning
- ▶ Different cyclical behaviors

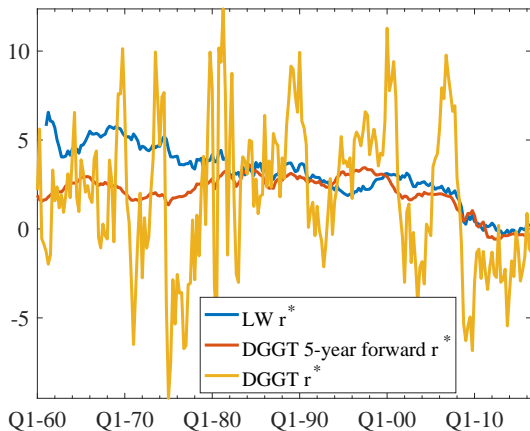
## Comment 4: Model dependent results



- ▶ For the first 70% of the sample, the correlation is -0.57
- ▶ The difference was 4.8% at the largest

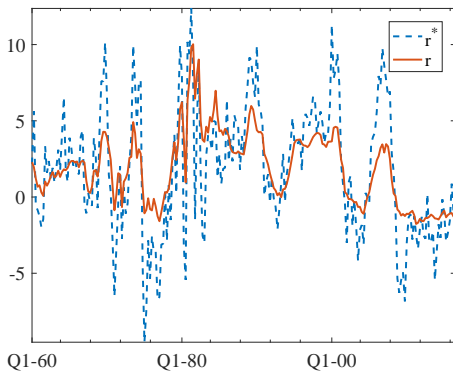


## Comment 4: Model dependent results



- ▶  $r^*$  is much more volatile than the other two series
- ▶ There is hardly a common pattern across the three

Comment 4: Should the natural rate of interest be more volatile than observed rates?



The variance of  $r^*$  is 3 times the variance of  $r$ .

# Conclusion

Overall, this is a very interesting, timely, and well written paper!

- ▶ Comment 1: downward trend in expectation.
- ▶ Comment 2: is very negative nominal  $r^*$  a shadow rate?
- ▶ Comment 3: there isn't a trend in convenience yield in the data.
- ▶ Comment 4: model dependent results.