



The 2004 Brown Center Report  
on American Education:

# HOW WELL ARE AMERICAN STUDENTS LEARNING?

*With studies of NAEP math  
items, middle school math  
teachers, and the revamped  
Blue Ribbon Schools awards*

THE BROOKINGS INSTITUTION

Part

I

# THE NATION'S ACHIEVEMENT/ NAEP MATH ITEMS



**Sample rubric from Singapore math curriculum**  
(grade levels at which skills are taught)

**Table**

**1-1**

<b>Operations on Whole Numbers</b>	<b>1A (1.0)</b>	<b>1B (1.5)</b>	<b>2A (2.0)</b>	<b>2B (2.5)</b>	<b>3A (3.0)</b>	<b>3B (3.5)</b>
<b>Addition/subtraction of 2-digit numbers within 20</b>	X					
<b>Addition/subtraction of 2-digit numbers within 100</b>		X				
<b>Addition/subtraction of 3-digit numbers</b>			X			
<b>Addition/subtraction of 4-digit numbers</b>					X	

Source: Primary Mathematics U.S. Edition Scope and Sequence for Singapore Math Curriculum,  
[http://www.singaporemath.com/scope\\_and\\_sequence\\_USedition\\_PriMath.htm](http://www.singaporemath.com/scope_and_sequence_USedition_PriMath.htm)

**When are key skills taught?**  
(comparing the study's rubric and state frameworks)

**Table**

**1-2**

	Study's Rubric	California	North Carolina	Massachusetts	Florida
<b>Whole Numbers</b>					
Addition/subtraction of whole numbers less than 100	1	1-2	1	1-2	1-2
Addition/subtraction of 3- and 4-digit numbers	2-3	2-3	2-3	2-3	3
Multiplication times tables and corresponding division facts	2-3	2-3	3	3	4
Multiplication/division of 3-digit number by 1-digit number	3	3	3-4	3-4	4
Division of up to a 4-digit number by a 2-digit number	5	5	4	5	5
<b>Fractions</b>					
Halves and quarters	1	2	2	1-2	1
Comparing and ordering unlike fractions	3	4	3	3-4	3
Addition/subtraction of related fractions	4	4	4	3-4	4
Addition/subtraction of unrelated fractions	5	5	5	5	4
Product of fractions	5	5	6	5-6	5
Division of a fraction by a whole number	5	5-6	6	5-6	5
<b>Percentages</b>					
Concepts and computing (with) percentages	5-6	5-6	6	5-7	5-6

Source: Data compiled from respective state department of education websites;  
Primary Mathematics U.S. Edition Scope and Sequence for Singapore Math Curriculum,  
[http://www.singaporemath.com/scope\\_and\\_sequence\\_USedition\\_PriMath.htm](http://www.singaporemath.com/scope_and_sequence_USedition_PriMath.htm)

**Problem solving items with arithmetic**  
(by grade level of item)

**Table**

**1-3**

*4th Grade*

<b>Grade Level</b>	<b>N</b>	<b>Students Answering Correctly (%)</b>	<b>Standard Error</b>	<b>Minimum</b>	<b>Maximum</b>
<b>1st</b>	<b>6</b> (15.4%)	<b>49.7</b>	<b>8.2</b>	<b>25</b>	<b>78</b>
<b>2nd</b>	<b>11</b> (28.2%)	<b>41.7</b>	<b>4.9</b>	<b>9</b>	<b>66</b>
<b>3rd</b>	<b>8</b> (20.5%)	<b>31.6</b>	<b>3.4</b>	<b>20</b>	<b>47</b>
<b>4th</b>	<b>11</b> (28.2%)	<b>28.8</b>	<b>4.4</b>	<b>8</b>	<b>58</b>
<b>5th</b>	<b>3</b> (7.7%)	<b>30.7</b>	<b>10.2</b>	<b>20</b>	<b>51</b>

Note: N= 39, Mean grade level: 3.1, Mean percent of students answering correct: 36.4

*8th Grade*

<b>Grade Level</b>	<b>N</b>	<b>Students Answering Correctly (%)</b>	<b>Standard Error</b>	<b>Minimum</b>	<b>Maximum</b>
<b>1st</b>	<b>7</b> (16.3%)	<b>54.0</b>	<b>8.4</b>	<b>25</b>	<b>92</b>
<b>2nd</b>	<b>10</b> (23.3%)	<b>45.4</b>	<b>8.3</b>	<b>5</b>	<b>82</b>
<b>3rd</b>	<b>8</b> (18.6%)	<b>41.4</b>	<b>7.5</b>	<b>4</b>	<b>69</b>
<b>4th</b>	<b>8</b> (18.6%)	<b>32.6</b>	<b>8.7</b>	<b>6</b>	<b>73</b>
<b>5th</b>	<b>6</b> (13.9%)	<b>38.5</b>	<b>6.6</b>	<b>17</b>	<b>58</b>
<b>6th</b>	<b>1</b> (2.3%)	<b>NA</b>	<b>NA</b>	<b>NA</b>	<b>NA</b>
<b>7th</b>	<b>3</b> (7.0%)	<b>27.7</b>	<b>9.3</b>	<b>13</b>	<b>45</b>

Notes: N= 43, Mean grade level: 3.4, Mean percent of students answering correct: 41.4  
The single sixth grade item is constructed response.

Source: Author's work and NAEP question tool <http://nces.ed.gov/nationsreportcard/ITMRLS/pickone.asp>

**Summary of achievement and grade level of  
problem solving items (by content strands)**

**Table**

**1-4**

*4th Grade*

<b>Content Strand</b>	<b>N</b>	<b>Items with Whole Numbers Only</b>	<b>Average Grade Level of Items</b>	<b>Students Answering Correctly (%)</b>
<b>Algebra</b>	<b>5</b>	<b>5</b> (100%)	<b>2.3</b>	<b>24.4</b>
<b>Data analysis</b>	<b>3</b>	<b>2</b> (66.7%)	<b>2.5</b>	<b>45.3</b>
<b>Geometry</b>	<b>0</b>	<b>NA</b>	<b>NA</b>	<b>NA</b>
<b>Measurement</b>	<b>6</b>	<b>4</b> (66.7%)	<b>2.8</b>	<b>37.3</b>
<b>Number sense</b>	<b>25</b>	<b>17</b> (48.6%)	<b>3.4</b>	<b>37.5</b>
<b>Total</b>	<b>39</b>	<b>28</b> (71.8%)	<b>3.1</b>	<b>36.4</b>

*8th Grade*

<b>Content Strand</b>	<b>N</b>	<b>Items with Whole Numbers Only</b>	<b>Average Grade Level of Items</b>	<b>Students Answering Correctly (%)</b>
<b>Algebra</b>	<b>8</b>	<b>7</b> (87.5%)	<b>2.4</b>	<b>37.0</b>
<b>Data analysis</b>	<b>2</b>	<b>1</b> (50.0%)	<b>4.5</b>	<b>33.5</b>
<b>Geometry</b>	<b>5</b>	<b>5</b> (100%)	<b>3.2</b>	<b>22.6</b>
<b>Measurement</b>	<b>10</b>	<b>5</b> (50.0%)	<b>3.7</b>	<b>37.4</b>
<b>Number sense</b>	<b>18</b>	<b>12</b> (66.7%)	<b>3.6</b>	<b>49.4</b>
<b>Total</b>	<b>43</b>	<b>30</b> (69.8%)	<b>3.4</b>	<b>40.4</b>

Source: Analysis of NAEP items in public release.

Data on items available at <http://nces.ed.gov/nationsreportcard/ITMRLS>



## Comparison of algebra and number sense items

Table

1-5

### 4th Grade

Content Strand	N	Items with Whole Numbers Only	Average Grade Level of Items	Students Answering Correctly (%)
Algebra	15	15 (100%)	2.3	40.5
Number sense	66	47 (71.2%)	3.4	48.1

### 8th Grade

Content Strand	N	Items with Whole Numbers Only	Average Grade Level of Items	Students Answering Correctly (%)
Algebra	25	23 (92.0%)	2.6	45.6
Number sense	54	31 (57.4%)	4.1	55.3

Source: Analysis of NAEP items in public release.

Data on items available at <http://nces.ed.gov/nationsreportcard/ITMRLS>

## Comparison of algebra and number sense items

(by calculator use)

Table

1-6

### 4th Grade

Content Strand	Calculator?	N	Items with Whole Numbers Only	Average Grade Level
Algebra	Y	8	100%	2.9
	N	7	100%	1.6
Number sense	Y	27	70.4%	3.8
	N	39	71.8%	3.1

### 8th Grade

Content Strand	Calculator?	N	Items with Whole Numbers Only	Average Grade Level
Algebra	Y	10	80.0%	3.4
	N	15	100%	2.1
Number sense	Y	21	42.9%	4.7
	N	33	66.7%	3.6

Source: Analysis of NAEP items in public release.

Data on items available at <http://nces.ed.gov/nationsreportcard/ITMRLS>



**Grade 4 Item Block: 2003-4M10 No. 8:**

$M=2$
$K=6$
$L=3$

**8. What is  $K + L - M$ ?**

- A) 1**
- B) 5**
- C) 7**
- D) 11**

**Grade 4 Block: 2003-4M6 No. 8**

8. Peter wrote down a pattern of A's and B's that repeats in groups of 3. Here is the beginning of his pattern with some of the letters erased. Fill in the missing letters.

**A** **B** \_ **A** \_ **B** \_ \_ \_

**Grade 8 Item Block: 1990-8M9 No. 8:**

**(2,5), (4,9), (6,13)**

Which of the following describes what to do to the first number in each ordered pair shown above to obtain the corresponding second number?

- A) Add 3**
- B) Subtract 3**
- C) Multiply by 2**
- D) Multiply by 2 and subtract 1**
- E) Multiply by 2 and add 1**

Part

II

# THE CONTENT TRAINING OF MIDDLE SCHOOL MATH TEACHERS



## Middle school math teacher backgrounds

Table

2-1

---

**Background**

**Percent**

---

**Undergraduate major  
in mathematics**

**22%**

**Undergraduate minor  
in mathematics**

**19%**

**Teaching credential  
or certificate in  
mathematics**

**41%**

**Middle school math  
teachers were asked:**

**Table**

**2-2**

**“In college, how many math courses  
did you complete that were offered  
by the mathematics department—  
not offered by the education school/  
department?”**

---

**Completed Courses**

**Percent**

---

**Four or more**

**77%**

**Three**

**7%**

**Two**

**7%**

**One**

**5%**

**None**

**4%**



**Middle school math  
teachers were asked:**

**Table**

**2-3**

**“In college, how many math courses  
did you complete that were  
offered by the education school/  
department—not offered by  
the mathematics department?”**

---

**Completed Courses**

**Percent**

---

**Four or more**

**17%**

**Three**

**9%**

**Two**

**26%**

**One**

**22%**

**None**

**24%**

**Percent of middle  
school mathematics  
teachers completing  
various college courses**

**Table**

**2-4**

<b>Completed Courses</b>	<b>Percent</b>
<b>General methods of teaching</b>	<b>92%</b>
<b>Methods of teaching mathematics</b>	<b>78%</b>
<b>Supervised student teaching in mathematics</b>	<b>47%</b>
<b>Mathematics for middle school teachers</b>	<b>45%</b>
<b>Instructional uses of computers/other technologies</b>	<b>43%</b>
<b>Geometry for elementary/ middle school teachers</b>	<b>36%</b>
<b>College algebra/trigonometry/ elementary functions</b>	<b>66%</b>
<b>Probability and statistics</b>	<b>56%</b>
<b>Geometry</b>	<b>47%</b>
<b>Computer programming or other computer science</b>	<b>45%</b>
<b>Calculus</b>	<b>43%</b>

**Percent of middle  
school mathematics  
teachers completing  
various college courses**

**Table**

**2-4**

<b>Completed Courses</b>	<b>Percent</b>
<b>Linear algebra</b>	<b>28%</b>
<b>Number theory</b>	<b>27%</b>
<b>Applications of mathematics/ problem solving</b>	<b>27%</b>
<b>Other upper division mathematics</b>	<b>25%</b>
<b>Abstract algebra</b>	<b>22%</b>
<b>Advanced calculus</b>	<b>21%</b>
<b>Differential equations</b>	<b>19%</b>
<b>History of mathematics</b>	<b>16%</b>
<b>Discrete mathematics</b>	<b>12%</b>
<b>Real analysis</b>	<b>11%</b>
<b>Engineering (any)</b>	<b>6%</b>

Source: Dawayne Whittington, "Status of Middle School Mathematics Teaching," (Horizon Research, Inc., December 2002), p. 4.

**Middle school math teachers were asked to describe their teaching responsibilities in a single day**

**Table**

**2-5**

---

**Responsibilities**

**Percent**

---

**All math courses**

**75%**

**Mostly math courses**

**17%**

**Some math courses**

**8%**

**No math courses**

**0%**

## Amount of professional development reported during the past two school years

Table

2-6

	No time	Less than 1 hour	1-2 hours	3-5 hours	More than 5 hours
Geometry	43%	15%	15%	9%	17%
Algebra	29%	10%	18%	10%	32%
Fractions and arithmetic	44%	14%	17%	9%	17%
Use of hands-on materials	23%	10%	23%	16%	28%
Integrating math topics	32%	13%	21%	12%	21%
Use of calculators	43%	12%	16%	11%	18%
Writing in math	33%	19%	23%	11%	13%
Math projects	47%	13%	20%	9%	11%
State standards	15%	9%	19%	13%	44%

**Number of topics on  
which teachers  
received professional  
development**

**Table**

**2-7**

---

<b>Number of Topics</b>	<b>Percent of Teachers</b>
<b>None</b>	<b>3%</b>
<b>1-3 topics</b>	<b>16%</b>
<b>4-7 topics</b>	<b>44%</b>
<b>8 or more topics</b>	<b>36%</b>



Teachers were asked to evaluate professional development they've received during the past two years.

Table

2-8

	Not helpful	Somewhat helpful	Very helpful
Geometry	14%	57%	29%
Algebra	5%	54%	41%
Fractions and arithmetic	11%	56%	33%
Use of hands-on materials	8%	52%	40%
Integrating math topics	21%	52%	27%
Use of calculators	15%	44%	41%
Writing in math	17%	54%	29%
Math projects	29%	53%	18%
State standards	12%	48%	39%

Responses from teachers who have participated in professional development

## Education and teaching assignments of teachers with high, middle, and low levels of content training

Table

2-11

	Low (n=56)	Middle (n=133)	High (n=53)
4 or more education courses	23.6	18.3	9.3
Math credential	17.9	60.3	61.1
Full time	53.6	83.8	77.8

**Percentage of teachers reporting 5 or more hours of professional development on various topics during the past two years, by level of content knowledge**

**Table**

**2-12**

	<b>Low</b>	<b>Medium</b>	<b>High</b>
<b>Geometry</b>	<b>18%</b>	<b>18%</b>	<b>11%</b>
<b>Algebra</b>	<b>33%</b>	<b>33%</b>	<b>30%</b>
<b>Fractions and arithmetic</b>	<b>18%</b>	<b>17%</b>	<b>9%</b>
<b>Use of hands-on materials</b>	<b>31%</b>	<b>27%</b>	<b>23%</b>
<b>Integrating math topics</b>	<b>25%</b>	<b>20%</b>	<b>17%</b>
<b>Use of calculators</b>	<b>13%</b>	<b>20%</b>	<b>19%</b>
<b>Writing in math</b>	<b>9%</b>	<b>14%</b>	<b>11%</b>
<b>Math projects</b>	<b>13%</b>	<b>7%</b>	<b>15%</b>
<b>State standards</b>	<b>42%</b>	<b>48%</b>	<b>38%</b>

**Percentage of teachers who would find professional development on the following topics “Very helpful,” by level of content knowledge**

**Table**

**2-13**

	<b>Low</b>	<b>Medium</b>	<b>High</b>
<b>Geometry</b>	<b>51%</b>	<b>40%</b>	<b>26%</b>
<b>Algebra</b>	<b>60%</b>	<b>47%</b>	<b>34%</b>
<b>Fractions and arithmetic</b>	<b>45%</b>	<b>33%</b>	<b>19%</b>
<b>Use of hands-on materials</b>	<b>47%</b>	<b>45%</b>	<b>30%</b>
<b>Integrating math topics</b>	<b>52%</b>	<b>46%</b>	<b>32%</b>
<b>Use of calculators</b>	<b>51%</b>	<b>38%</b>	<b>26%</b>
<b>Writing in math</b>	<b>44%</b>	<b>39%</b>	<b>25%</b>
<b>Math projects</b>	<b>45%</b>	<b>45%</b>	<b>36%</b>
<b>State standards</b>	<b>38%</b>	<b>41%</b>	<b>23%</b>

**Middle school math teachers were asked: “Which of the following incentives do you think would be effective in persuading teachers to attend a summer institute?”**

**Table**

**2-14**

	Not effective	Somewhat effective	Very effective
Extra pay or stipend	0%	13%	87%
Salary schedule advancement	2%	18%	80%
Credits toward a degree	7%	36%	58%
Credit for leave or release time	22%	38%	40%

Part



# BLUE RIBBON SCHOOLS





## Achievement of 1999 Blue Ribbon Schools (1999 test scores)

Table

3-1

*Percentile*

State	Number	99th-90th	89th-50th	49th-1st
California	39	12 (31%)	18 (46%)	9 (23%)
Illinois	3	1 (33%)	1 (33%)	1 (33%)
Indiana	4	0 (0%)	2 (50%)	2 (50%)
Michigan	9	1 (11%)	5 (56%)	3 (33%)
Pennsylvania	10	4 (40%)	6 (60%)	0 (0%)
New Mexico	1	0 (0%)	0 (0%)	1 (100%)
Washington	4	1 (25%)	2 (50%)	1 (25%)
Total	70	19 (27%)	34 (49%)	17 (24%)

Note: Test scores from 1998-1999 school year, adjusted for socioeconomic status (SES). Public schools only. Blue Ribbon awards given in 1999.

Source: Tom Loveless. *The Brown Center Report on American Education: How Well Are American Students Learning?* (2000)

## Achievement of 1999 Blue Ribbon Schools (2003 test scores)

Table

3-2

*Percentile*

State	Number	99th-90th	89th-50th	49th-1st
California	38	2 (5%)	30 (79%)	6 (16%)
Illinois	3	0 (0%)	3 (100%)	0 (0%)
Indiana	4	0 (0%)	3 (75%)	1 (25%)
Michigan	9	0 (0%)	6 (67%)	3 (33%)
Pennsylvania	10	2 (20%)	7 (70%)	1 (10%)
Washington	4	0 (0%)	3 (75%)	1 (25%)
<b>Total</b>	<b>68</b>	<b>4 (6%)</b>	<b>52 (76%)</b>	<b>12 (18%)</b>

Note: Test scores from 2002-2003 school year, adjusted for socioeconomic status (SES). Public schools only. Blue Ribbon awards given in 1999.

Source: Data compiled from respective state department of education websites.

## Achievement of 2003 Blue Ribbon Schools (2003 test scores)

Table

3-3

*Percentile*

State	Number	99th-90th	89th-50th	49th-1st
California	24	2 (8%)	18 (75%)	4 (17%)
Illinois	6	1 (17%)	4 (66%)	1 (17%)
Indiana	3	2 (67%)	1 (33%)	0 (0%)
Missouri	8	5 (63%)	3 (37%)	0 (0%)
Pennsylvania	3	1 (33%)	2 (67%)	0 (0%)
Ohio	10	7 (70%)	3 (30%)	0 (0%)
Washington	3	0 (0%)	3 (100%)	0 (0%)
Total	57	18 (31%)	34 (60%)	5 (9%)

Note: Test scores from 2002-2003 school year, adjusted for socioeconomic status (SES). Public schools only. Blue Ribbon awards given in 2003.

Source: Data compiled from respective state department of education websites.