

# Measuring method performance in prospective safety monitoring

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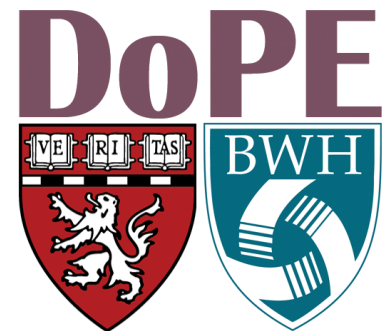
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# Objectives of monitoring methods

- Identify all safety issues of interest (sensitivity)
- Produce as few false positives as possible (specificity)
- But, in prospective monitoring, we also want:
  - True positives identified early and false positives identified late (if they are to occur at all)
  - Performance weighted differently in different scenarios

# Imagine the following scenarios...

- Hypothetical monitoring scenario 1:
  - Febrile seizures after administration of one type of vaccine (monitoring vaccine) versus another (comparison vaccine)
  - Monitoring vaccine increases febrile seizure risk by 2-fold
- Hypothetical monitoring scenario 2:
  - AMI in users of an anti-diabetic drug (monitoring drug) versus users of another anti-diabetic drug (comparison drug)
  - Monitoring drug does not increase AMI risk
- Two hypothetical monitoring methods could be used
- New data become available on a quarterly basis, for a total of 10 periods

# Hypothetical febrile seizure data

1:1  
match

## Numbers of new febrile seizure observed in each quarter

	1	2	3	4	5	6	7	8	9	10	Total
<b>Monitoring vaccine</b>	20	20	20	20	20	20	20	20	20	20	200
<b>Comparison vaccine</b>	10	10	10	10	10	10	10	10	10	10	100

# Hypothetical febrile seizure data

Numbers of new febrile seizure observed in each quarter											
	1	2	3	4	5	6	7	8	9	10	Total
1:1 match	<b>Monitoring vaccine</b>	20	20	20	20	20	20	20	20	20	200
	<b>Comparison vaccine</b>	10	10	10	10	10	10	10	10	10	100

Method A

# Hypothetical febrile seizure data

Numbers of new febrile seizure observed in each quarter											
	1	2	3	4	5	6	7	8	9	10	Total
1:1 match	<b>Monitoring vaccine</b>	20	20	20	20	20	20	20	20	20	200
	<b>Comparison vaccine</b>	10	10	10	10	10	10	10	10	10	100

Method A

Method B

# Hypothetical AMI data



Numbers of new AMI observed in each quarter												
	1	2	3	4	5	6	7	8	9	10	Total	
1:1 match	<b>Monitoring drug</b>	12	12	12	8	8	8	13	9	8	10	100
	<b>Comparison drug</b>	9	10	8	10	10	11	9	12	11	10	100

# Hypothetical AMI data



Numbers of new AMI observed in each quarter												
	1	2	3	4	5	6	7	8	9	10	Total	
1:1 match	<b>Monitoring drug</b>	12	12	12	8	8	8	13	9	8	10	100
	<b>Comparison drug</b>	9	10	8	10	10	11	9	12	11	10	100

Method A



# Hypothetical AMI data

Numbers of new AMI observed in each quarter												
	1	2	3	4	5	6	7	8	9	10	Total	
1:1 match	<b>Monitoring drug</b>	12	12	12	8	8	8	13	9	8	10	100
	<b>Comparison drug</b>	9	10	8	10	10	11	9	12	11	10	100

Method A

Method B

# Hypothetical AMI data

Numbers of new AMI observed in each quarter												
	1	2	3	4	5	6	7	8	9	10	Total	
1:1 match	Monitoring drug	12	12	12	8	8	8	13	9	8	10	100
	Comparison drug	9	10	8	10	10	11	9	12	11	10	100

Method B

Method A

Method result

+  
-

Truth

+

-

1	1
0	0

Sensitivity = 1.00

Specificity = 0.00

# An event-based approach

Numbers of exposed events in each scenario in each quarter											
	1	2	3	4	5	6	7	8	9	10	Total
Scenario 1 (vaccine)	20	20	20	20	20	20	20	20	20	20	200
Scenario 2 (drug)	12	12	12	8	8	8	13	9	8	10	100

# An event-based approach

Numbers of exposed events in each scenario in each quarter											
	1	2	3	4	5	6	7	8	9	10	Total
<b>Scenario 1 (vaccine)</b>	20	20	20	20	20	20	20	20	20	20	200
<b>Scenario 2 (drug)</b>	12	12	12	8	8	8	13	9	8	10	100

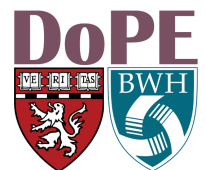
## Method A

Truth

		+	-
Method result	+	180	27
	-	20	73

Event-based sensitivity = 0.90

Event-based specificity = 0.73



# An event-based approach

Numbers of exposed events in each scenario in each quarter											
	1	2	3	4	5	6	7	8	9	10	Total
<b>Scenario 1 (vaccine)</b>	20	20	20	20	20	20	20	20	20	20	200
<b>Scenario 2 (drug)</b>	12	12	12	8	8	8	13	9	8	10	100

## Method A

Truth

		+	-
Method result	+	180	27
	-	20	73

Event-based sensitivity = 0.90

Event-based specificity = 0.73

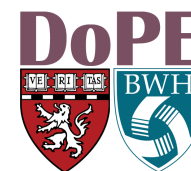
## Method B

Truth

		+	-
Method result	+	120	64
	-	80	36

Event-based sensitivity = 0.60

Event-based specificity = 0.36



# Event-based performance metric

$$EBP = \frac{\sum_{j=1}^n a_j \cdot w_j}{\sum_{j=1}^n a_j + c_j} + \frac{\sum_{j=1}^n d_j \cdot (1 - w_j)}{\sum_{j=1}^n d_j + b_j}$$

□ Where:

- $w_j$  = weight for sensitivity:specificity preference in scenario  $j$
- $n$  = total number of  $j$  scenarios

		Truth	
		+	-
Method result	+	$a_j$	$b_j$
	-	$c_j$	$d_j$

$j$

# A vs. B comparison with *EBP*

		Method A		Method B	
		Truth		Truth	
		+	-	+	-
Method result	+	180	27	120	64
	-	20	73	80	36
		Event-based sensitivity = 0.90		Event-based sensitivity = 0.60	
		Event-based specificity = 0.73		Event-based specificity = 0.36	

- $w_i = 0.1$  for febrile seizures;  $w_i = 0.2$  for AMI:
  - ▣  $EBP_{method\_A} = 0.674$  vs.  $EBP_{method\_B} = 0.348$
- $w_i = 0.01$  for febrile seizures;  $w_i = 0.01$  for AMI:
  - ▣  $EBP_{method\_A} = 0.731$  vs.  $EBP_{method\_B} = 0.362$

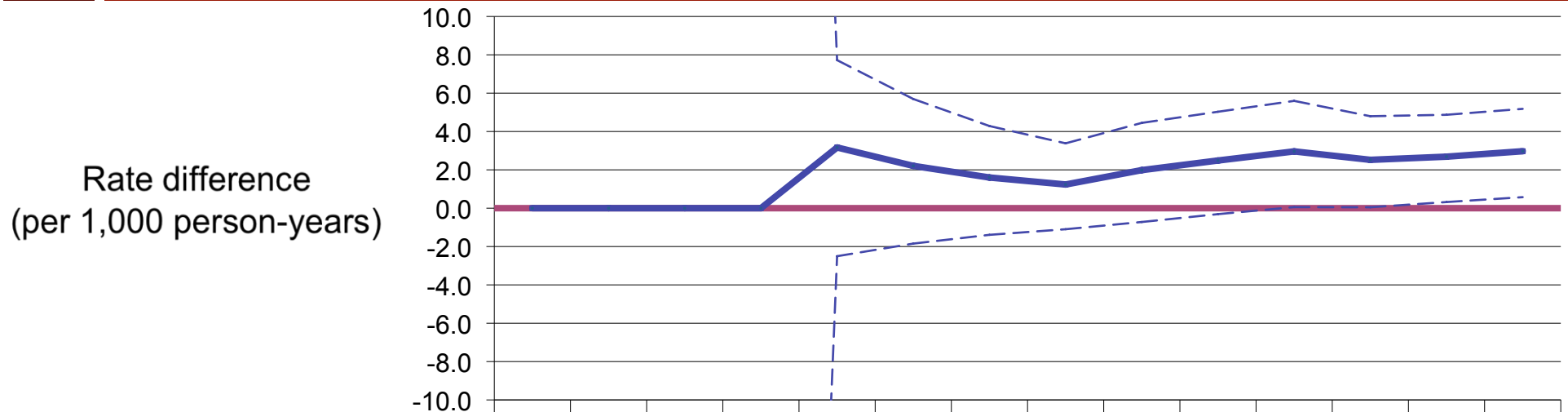
# Application in simulated data

- Simulated data resembling signal refinement for statin-induced rhabdomyolysis
- Assumed matched cohort design with 20 periods defined by calendar time (e.g. quarters)
- Compared 93 algorithms
- 100,000 iterations

$w_i$	Algorithm	Overall sensitivity	Overall specificity	EBP
0.01	maxSPRT ( $\alpha = 0.01$ )	0.18	1.00	0.99
0.10	Pocock-like spending function ( $\alpha = 0.10$ )	0.32	0.99	0.93
0.20	Pocock-like spending function ( $\alpha = 0.40$ )	0.49	0.95	0.87



# Translation to empirical data

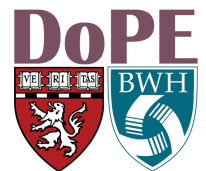


	1	2	3	4	5	6	7	8	9	10	11	12	13	14
--- Lower 95% confidence interval	-99.00	-99.00	-99.00	-99.00	-2.50	-1.85	-1.39	-1.10	-0.72	-0.31	0.06	0.05	0.32	0.58
— Cumulative rate difference	0.00	0.00	0.00	0.00	3.17	2.21	1.60	1.24	1.99	2.49	2.96	2.52	2.69	2.97
--- Upper 95% confidence interval	99.00	99.00	99.00	99.00	7.72	5.70	4.29	3.38	4.45	5.03	5.60	4.80	4.87	5.18
Cumulative exposed events	0	0	0	0	1	1	1	1	2	3	4	4	5	6
Cumulative unexposed events	0	0	0	0	0	0	0	0	0	0	0	0	0	0
Cumulative exposed person-years	19	60	124	197	316	453	625	809	1007	1206	1350	1586	1861	2019
Cumulative unexposed person-years	26	65	127	218	348	497	681	877	1084	1299	1462	1715	2010	2275

$w_i$	Algorithm	Alert period
0.01	maxSPRT ( $\alpha = 0.01$ )	--
0.10	Pocock-like spending function ( $\alpha = 0.10$ )	14
0.20	Pocock-like spending function ( $\alpha = 0.40$ )	11

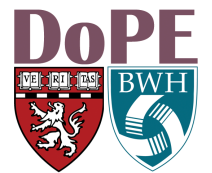
# Summary

- *EBP* is useful to compare performance of methods in settings in which truth is known
- Uses exposed events to incorporate time to signaling
  - ▣ Most relevant unit for public health decision making (i.e. modifiable)
  - ▣ The most meaningful measure of “time” in prospective monitoring
  - ▣ Main driver of statistical power
- Allows for transparent weighting of sensitivity-specificity tradeoffs that can vary by monitoring outcome
- Does not depend on “prevalence” of safety issues



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# Summarizing event-based performance

- Many ways to use events to summarize performance:
  - ▣ Mean average precision, diagnostic odds ratio,  $F_1$  score, Matthews correlation coefficient, Youden's J statistic, accuracy, etc.
  - ▣ All are functions of sensitivity, specificity, and (often) "prevalence"
  - ▣ Built-in tradeoffs between FP and FN costs are arbitrary and cannot be easily changed
- Sensitivity and specificity are characteristics of the methods whereas prevalence is arbitrary

