



**California Center for Population Research**  
**University of California - Los Angeles**

**Agent Models and  
Demographic Research**

**Robert D. Mare**

**December 7, 2007**

# **Agent Modeling vs. Business as Usual in Demographic Research**

## **Agent models**

**are inherently more complex than standard  
multivariate models**

**relax the assumption of independent and  
identically distributed (random) observations**

**relax the assumption that specific  
demographic rates are independent of  
population composition**

## **Interdependent Behaviors**

**Fertility, Mortality, Migration, Marriage, etc.**

**The rate at which you do it depends on how many and which other people are doing it.**

**(vs. classic approach in which the rate at which you do it depends only on your own characteristics.)**

## **Examples of Population-Dependent Rates**

- 1. Classic Macro Models of “Controlled” Populations  
(Lee, Easterlin, Samuelson, Malthus)  
(vs. stable models)**
- 2. Residential Choice “Interactive” Markov Models  
(Conlisk, Bruch-Mare, others)  
(vs. Markov models, such as Leslie matrix)**
- 3. Epidemics  
(Epstein, Morris, Moody, others)**

## **Examples of Population-Dependent Rates**

### **4. Diffusion of Demographic Innovations**

**European Fertility Decline (Coale et al.)**

**Language acquisition, maintenance, loss  
(Lieberson, Feldman & Cavalli-Sforza)**

### **5. Endogenous Policies**

- **Policing and crime**
- **Public health intervention and disease**

## **Examples of Population-Dependent Rates**

- 6. Policy effects where migration may be induced: e.g., welfare-magnet effects; homeless policy effects, etc.**
  
- 7. Incarceration, crime, wages, victimization, neighborhood poverty, socialization (elaborated prey-predator model) (Western)**

## **8. Formation of social units**

**Marriages (assortative mating)**

**Neighborhoods (Schelling, Bruch-Mare, Macy)**

**Peer Groups**

**Networks (Moody, others)**

**Kin, “kin availability,” social exchange  
(jointness of social relationships and  
spatial arrangements of kin)**

## **Issues**

**Theory, thought experiments, empirical work**

**Agent models are inherently complex**

**Give agents “real demography” (Lee, Axtell et. al.)  
Life cycles, aging, fertility, mortality,  
intergenerational transmission**

**Time horizons**

**Eons (Lee, Axtell et al.)**

**“Timeless” problems (Bruch-Mare, Macy)**

**What about finite periods (e.g., adolescence)?**

**How do we know how agents ought to act? (Stated  
vs. revealed preferences vs. make it up)**



**Hypothetical**

**Empirical**

**A**

**B**

**Simple**

**C**

**D**

**Complex**

## **Issues (continued)**

**Importance of aggregate data for “calibration”  
descriptive demography still matters**

### **Multi-actor models**

**Buyers, sellers, and real estate agents**

**Men, women, matchmakers**

**Adult children, elderly parents**

**Multiple influencers (parents, teachers, peers)**

**Multiple deciders (parents, students, colleges)**

**How smart should agents be? Can they learn??**

## **Issues (continued)**

**Can we combine studies of “outcomes”  
with studies of how social environments  
are created?**

**neighborhood effects**

**family structure effects**

**school effects**

**family background effects**



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# **Neighborhood Choice and Neighborhood Change**

**Elizabeth E. Bruch and Robert D. Mare**

*American Journal of Sociology*  
2006, pp. 667-709

## **Broad Goals:**

- **Investigate how inequality is affected by spatial arrangement of population.**
- **Investigate neighborhood effects when residential location is endogenous.**
- **Explain and forecast residential segregation.**
- **Investigate the relationship between geographic and social mobility.**

## **Two Approaches**

### **1. Residential Mobility and Neighborhood Change in L.A.**

**-Uses real data on actual mobility and residential demography**

### **2. Artificial Neighborhoods and Computational Models**

**- Investigates general principles about the effects of residential preferences and population composition on neighborhood change.**

**-Extends Schelling's work on residential tipping to**

- multi-ethnic cities**
- larger cities**
- residential sorting based on race and income**

## **Our Research**

- 1. Develop a model of geographic mobility and neighborhood change**
- 2. Link individuals' mobility decisions to their preferences for neighborhoods with varying race-ethnic makeup.**
- 3. Link the changing race-ethnic makeup of neighborhoods to mobility flows.**
- 4. Let the mobility decisions of each individual potentially alter the attractiveness of neighborhoods for all other individuals.**

## **Empirical Approach**

### **Los Angeles Survey of Families and Neighborhoods (residential mobility history)**

- Actual Mobility vs. Stated Preferences**
- Mobility in a Plausible Local Residential  
Opportunity Structure**



- **Discrete Choice Model**

**Neigh. Choice = F(Neigh. Char. x Individ. Char.)**

- **Use estimated choice function to predict movement between real neighborhoods (L.A. Census Tracts). (Interactive Markov Chain)**

## **Problems:**

- 1. So much data, so many possible regressions....**
- 2. What properties of choice function are particularly consequential for neighborhood change?**

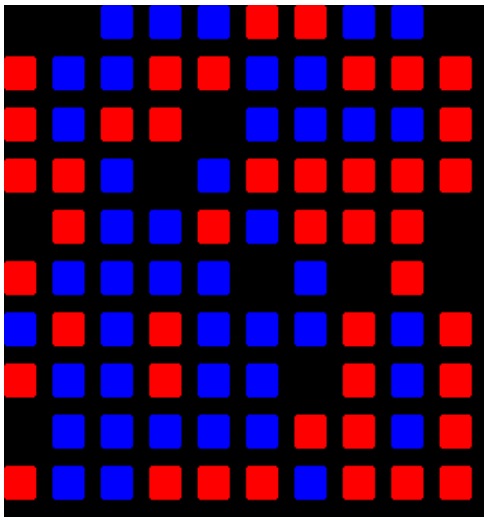
# Schelling

- **Simple threshold model**
- **Even mild preferences for own race produce high segregation**
- **Residential tipping**

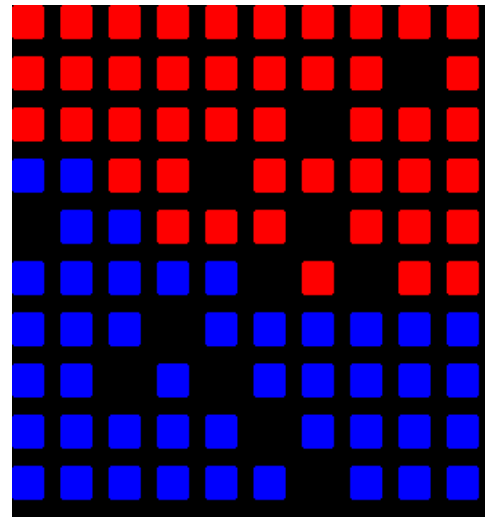
**But...**

- **Small world; 2 groups**
- **Hypothetical preference function; unrealistic assumptions about individual behavior**

# Schelling's Model



Start



End

# Typical Problems with ABMs

- **Models are often assumed without (a) empirical validation and (b) investigation of how alternative assumptions about individual behavior affect macro-level outcomes**

# Questions

- 1. What assumptions about individuals' race/ethnic preferences imply tipping?**
- 2. Do data on preferences support these assumptions?**

# Choice Model

## 1) Random Utility (McFadden)

- $U_{ijt} = F(Z_{jt}, X_{it}, \eta_{jt}, \varepsilon_{it})$

- $$p_{ijt}(Z_{jt}, X_{it}, C_{(i)}) = \frac{\exp(\beta_i^* Z_{jt} + \delta Z_{jt} X_{it} + \eta_{jt})}{\sum_{k \in C_{(i)}} \exp(\beta_i^* Z_{kt} + \delta Z_{kt} X_{it} + \eta_{kt})}$$

## **Special Features of Residential Choice**

- (a) “Inertia” (pref. for current residence)**
- (b) Restricted Choice Sets**
- (c) Preference Heterogeneity**
- (d) Size Restrictions on Neighborhood**
- (e) Endogenous Prices**
- (f) Dynamic Effects of Neighborhoods**
- (g) Dynamic Effects of Biography**



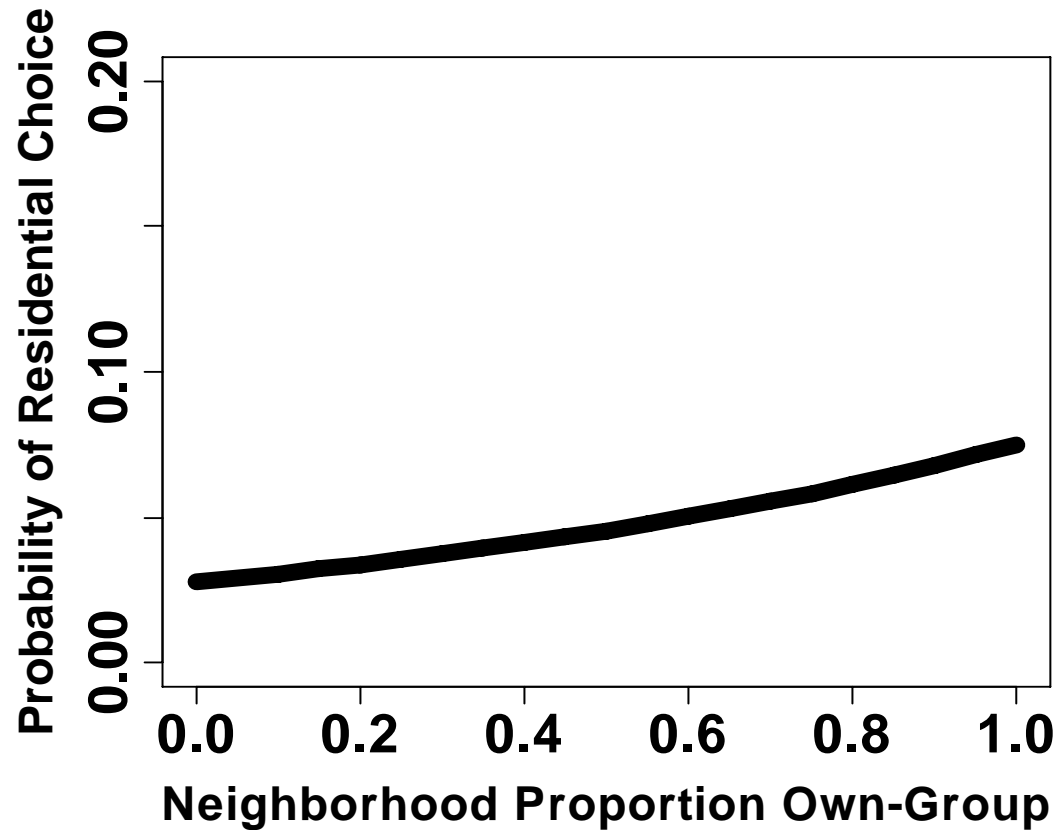
# Schelling Preference Function



$$\Pr(\text{moving into the } j^{\text{th}} \text{ neighborhood at time } t) = \frac{X_{jt}}{\sum_{k=1}^K X_{kt}}$$

$$X_{jt} = 1 \bullet \{\text{neighborhood proportion own group} \geq 0.5\}$$

# Continuous Function



$$\text{Pr}(\text{moving into the } j^{\text{th}} \text{ neighborhood at time } t) = \frac{e^{q_{jt}}}{\sum_{k=1}^K e^{q_{kt}}}$$

$q_{jt}$  = proportion own group in neighborhood  $j$  at time  $t$

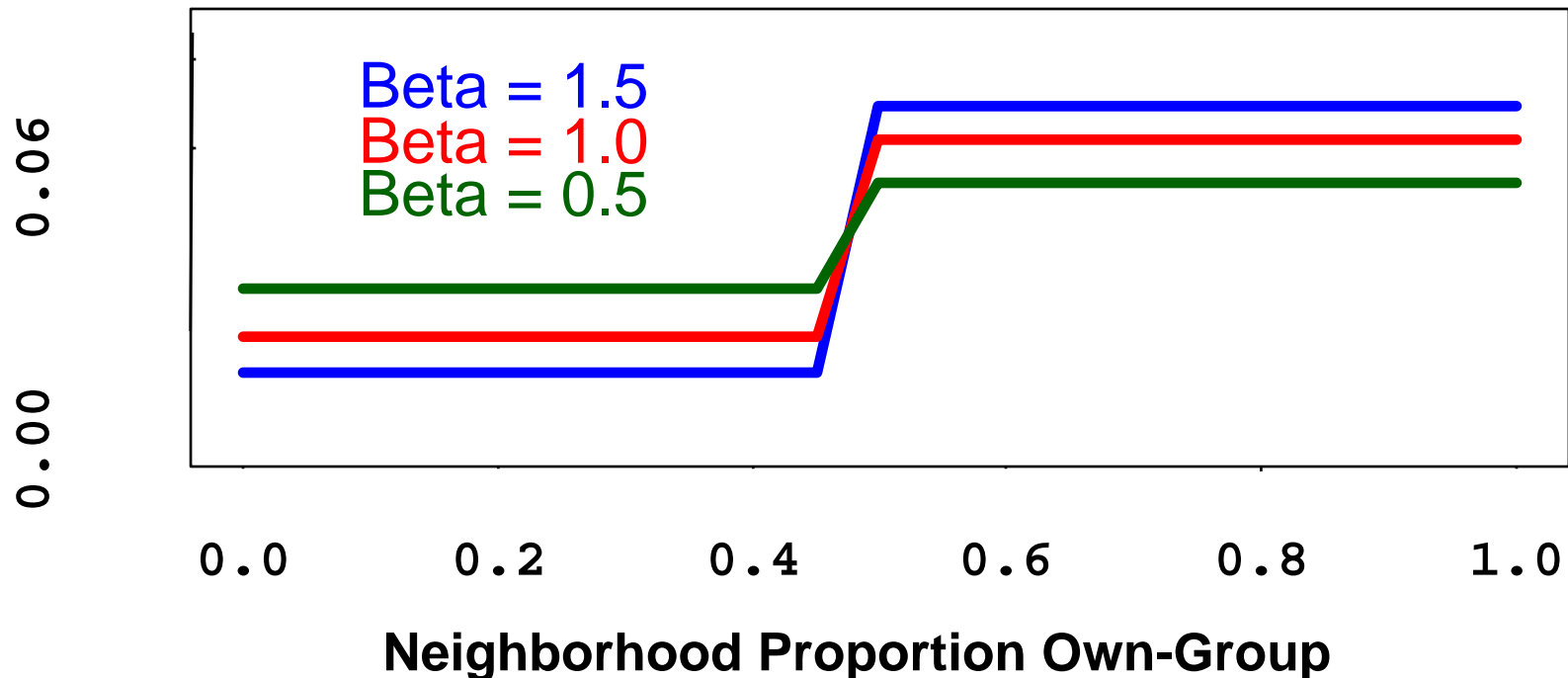
# Individual Heterogeneity

$$\Pr(i^{th} \text{ agent moves to the } j^{th} \text{ neighborhood at time } t) = \frac{e^{\beta_i * X_{ijt}}}{\sum_{k=1}^K e^{\beta_i * X_{ikt}}}$$

where  $X_{ijt} = 1 \bullet \{\text{neighborhood } j \text{ proportion own group} \geq 0.5\}$

and  $\beta_i \sim N(1, \sigma^2)$

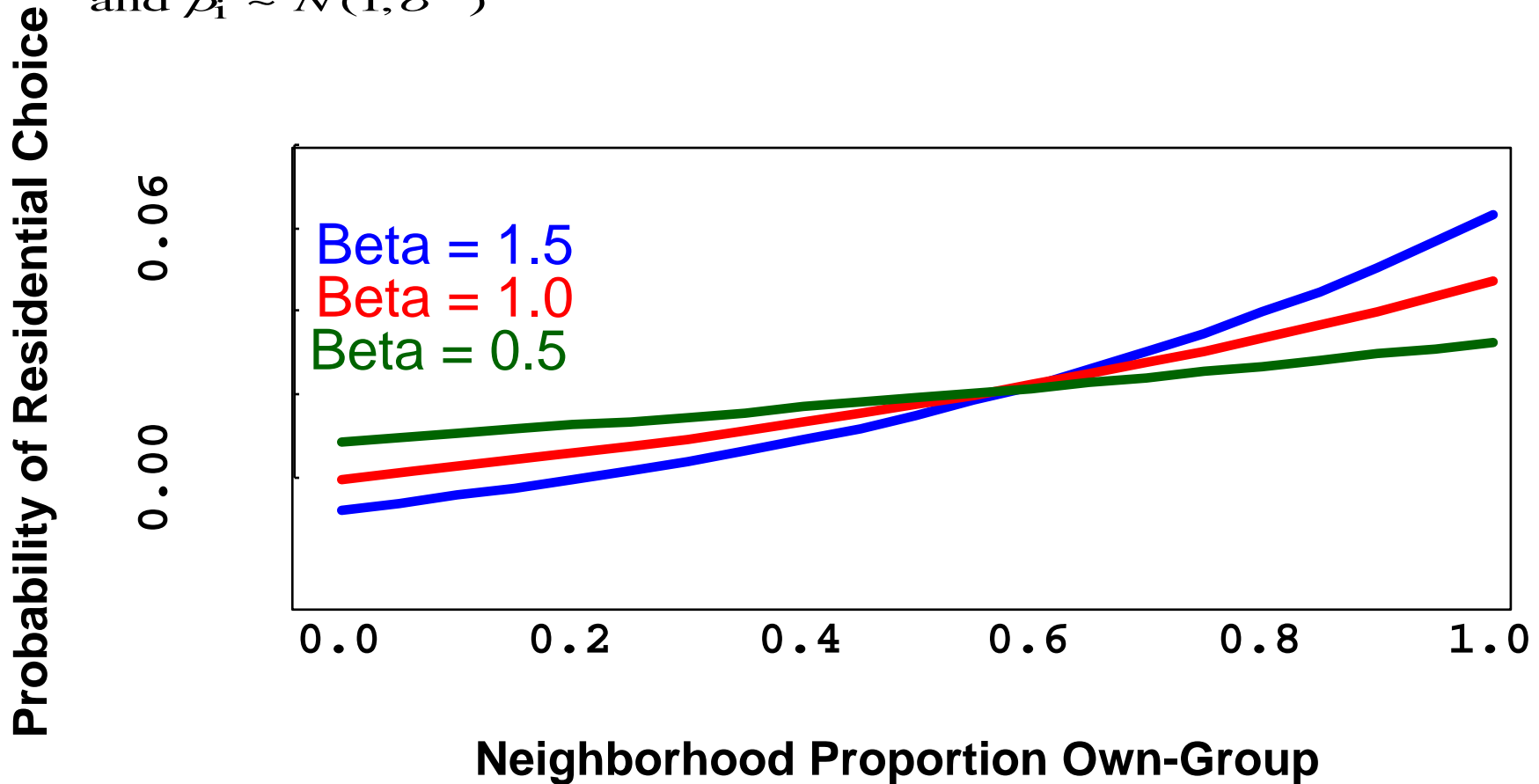
Probability of Residential Choice



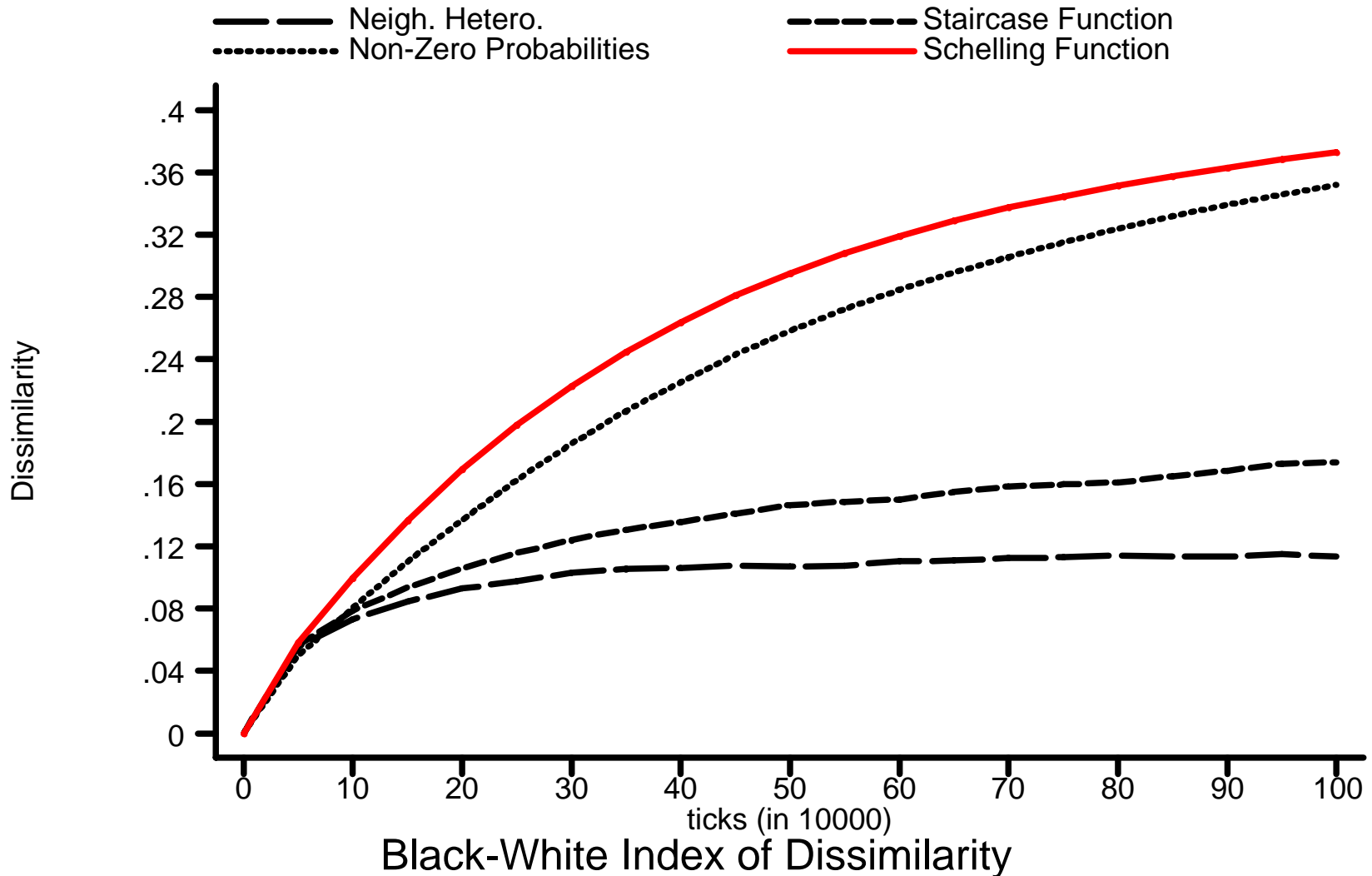
## Continuous Function, Individual Heterogeneity

$$\Pr(i^{th} \text{ agent moves to the } j^{th} \text{ neighborhood at time } t) = \frac{e^{\beta_i * q_{ijt}}}{\sum_{k=1}^K e^{\beta_i * q_{ikt}}}$$

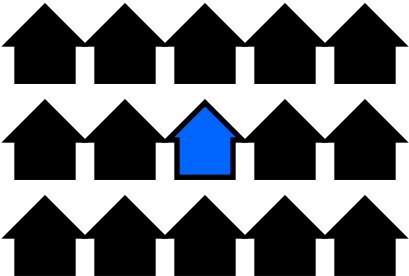
where  $q_{ijt}$  = proportion own group in  $j^{th}$  neighborhood at time  $t$   
and  $\beta_i \sim N(1, \sigma^2)$



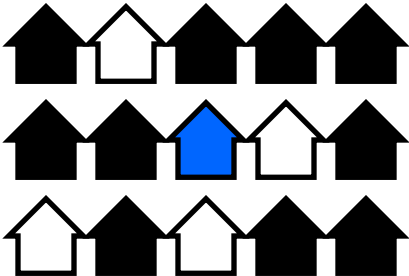
# Segregation Measures, Modified Schelling Preference Function



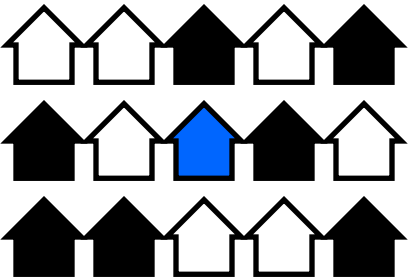
# Vignette Data -- DAS, MCSUI



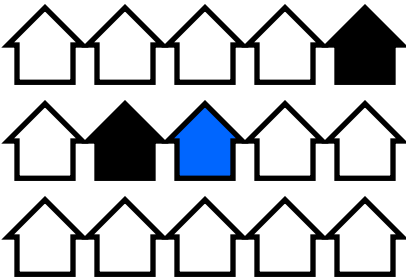
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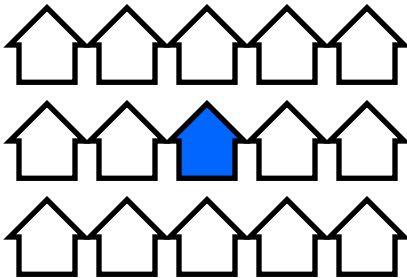
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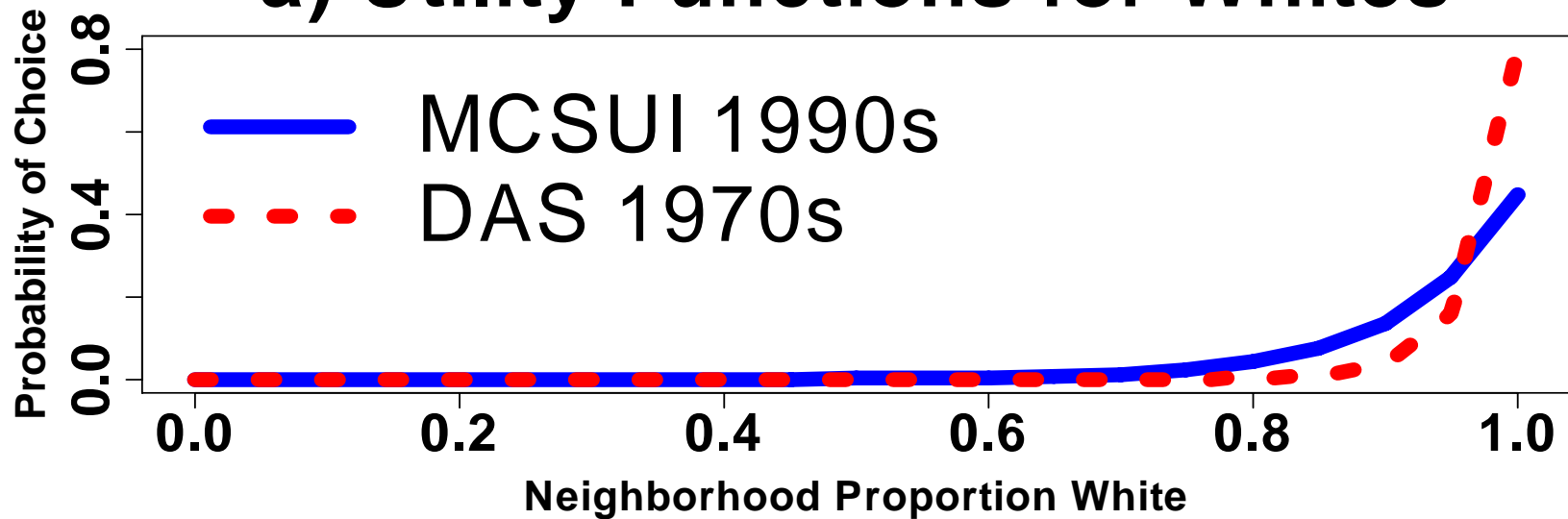
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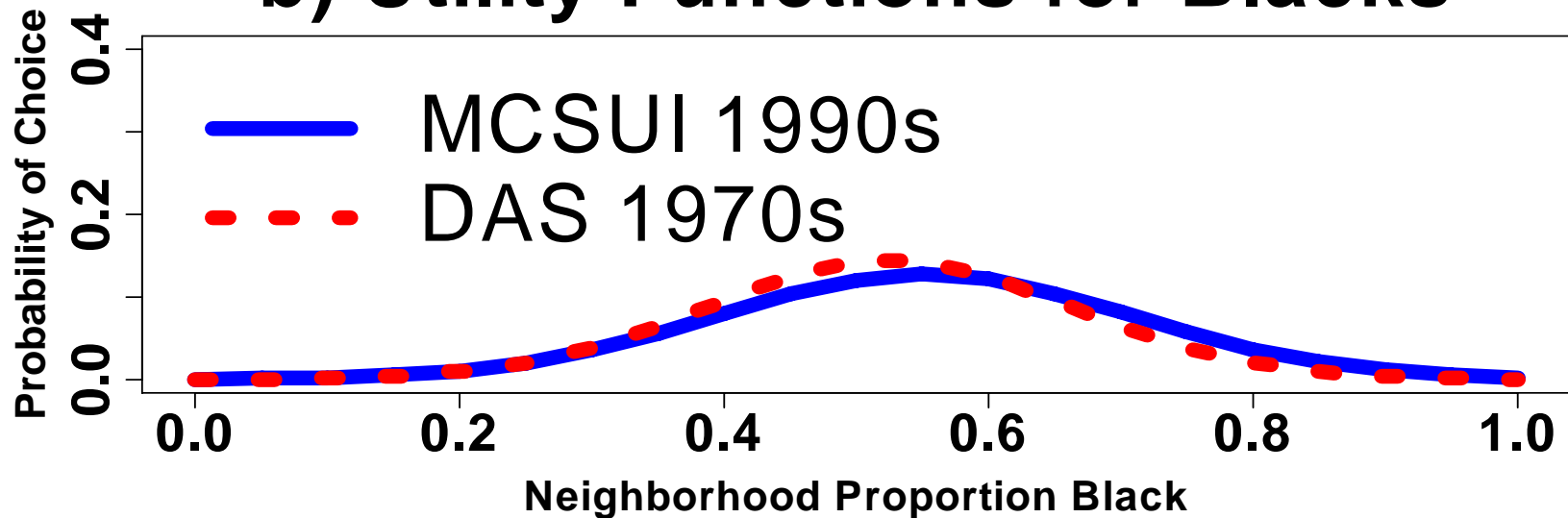
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# Empirical Functions, 1970s and 1990s

## a) Utility Functions for Whites



## b) Utility Functions for Blacks



# **Continuous Functions May Result in Low Segregation**

- **Small inflows of whites to minority white area make neighborhood increasingly attractive to whites. Neighborhood whitens *until whites in other neighborhoods are too few to create a large flow.***
- **Growing neighborhood attractiveness eventually offset by dwindling population at risk to entering neighborhood (and increasing population at risk to exiting).**



# **Threshold Functions Maintain High Segregation**

- With threshold models, small change in proportion own group may not be enough to increase neighborhood attractiveness.**
- Neighborhoods stabilize at either zero or low proportion minority group.**

# **Random Variability and Segregation**

**Whether Continuous Choice Functions for Individuals Lead to Low or High Segregation Depends on Degree of Randomness in Mobility Process**

**High randomness implies low segregation;  
Low randomness implies high segregation**

**Schelling's Model is (essentially) deterministic because neighborhoods with high own group proportion are an "absorbing state."**

# Next Steps

- **Design an agent-based model that is grounded in real world data on residential mobility and neighborhood change, and use it to simulate patterns of neighborhood change in race and income composition**
- **Develop statistical methods to assess how well this model captures trends in patterns of segregation and neighborhood turnover**
- **See Bruch (in progress)**

# **The Effects and Causes of Mixed Income Housing**

**(R. D. Mare and SSRC-MacArthur Mixed Income  
Research Design Group)**

## **Policies**

- **Redevelop Low Income to Mixed Income Housing (bring nonpoor to poor – but displace some poor)**
- **Housing Assistance Via Vouchers (bring poor to nonpoor – but possible nonpoor “flight”?)**

# Issues

- **Effects vs. Causes**
  - **Does income mixing have beneficial effects?**
  - **Is income mixing inherently desirable?**
  - **Is income mixing possible?**
- **Mixed Income Housing vs. Mixed Income Neighborhoods**
- **Policy Effects vs. Baseline Patterns of Income Mixing/Segregation**

## **Elements of Baseline Model:**

- **Cross Section Patterns of Income Segregation**
- **Rates of Residential Mobility Among Neighborhoods (by poor and nonpoor)**
- **Rates of Socioeconomic (Income) Mobility**
- **Equilibrium Income Segregation Implied by Mobility Rates**
- **Residential Mobility = F(income, neighborhood income composition, life cycle factors, market factors)**
- **Income Mobility = G(life cycle factors, neighborhood factors)**

# **Complications**

- **Immigration**
- **New Construction**
- **(Endogenous and Exogenous Social Policies)**
- **Social Factors (Race, Discrimination, Incarceration)**

## **Data Needs**

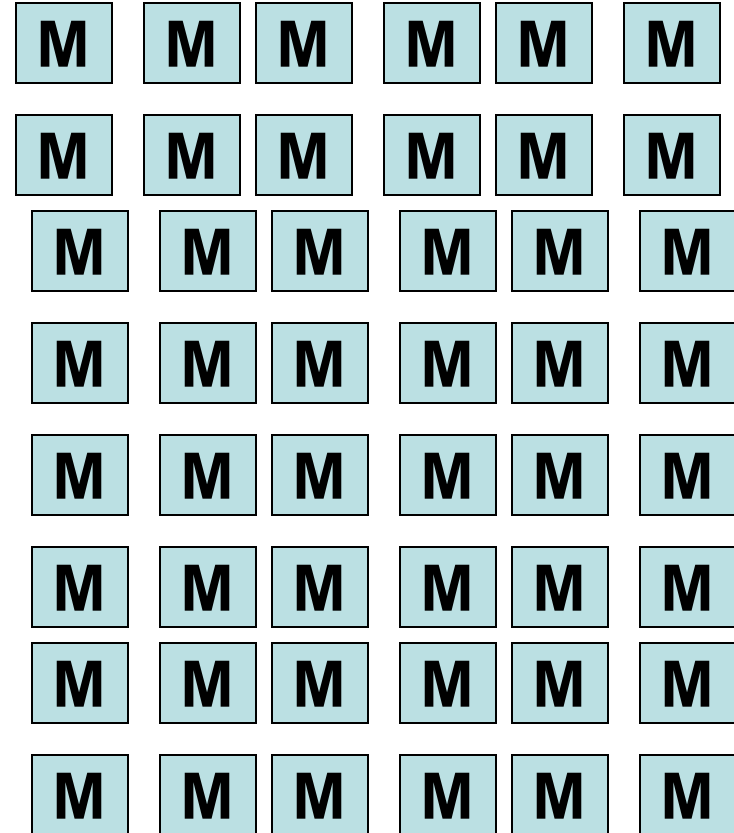
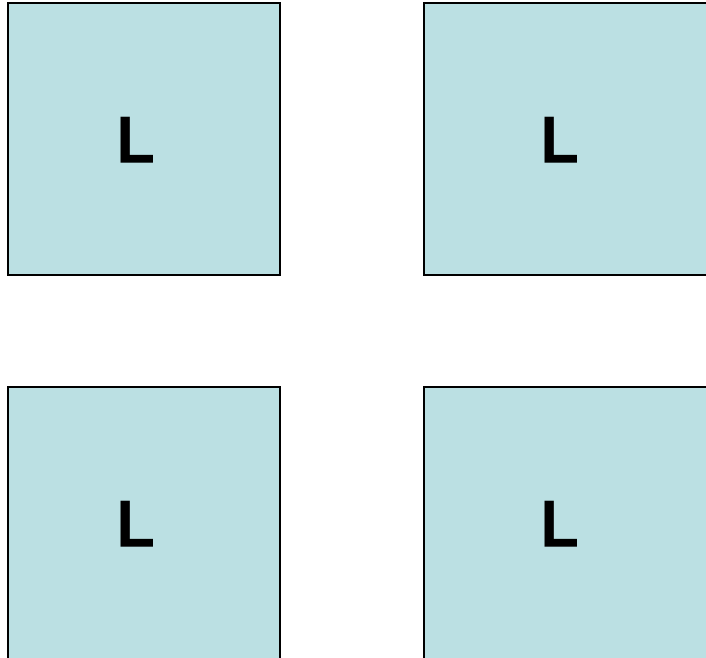
- **Cross Section Observations on Spatial Distribution of Income**
- **Longitudinal Observations on residential choice/mobility and income mobility**



## **Elements of a rudimentary “Policy Model”**

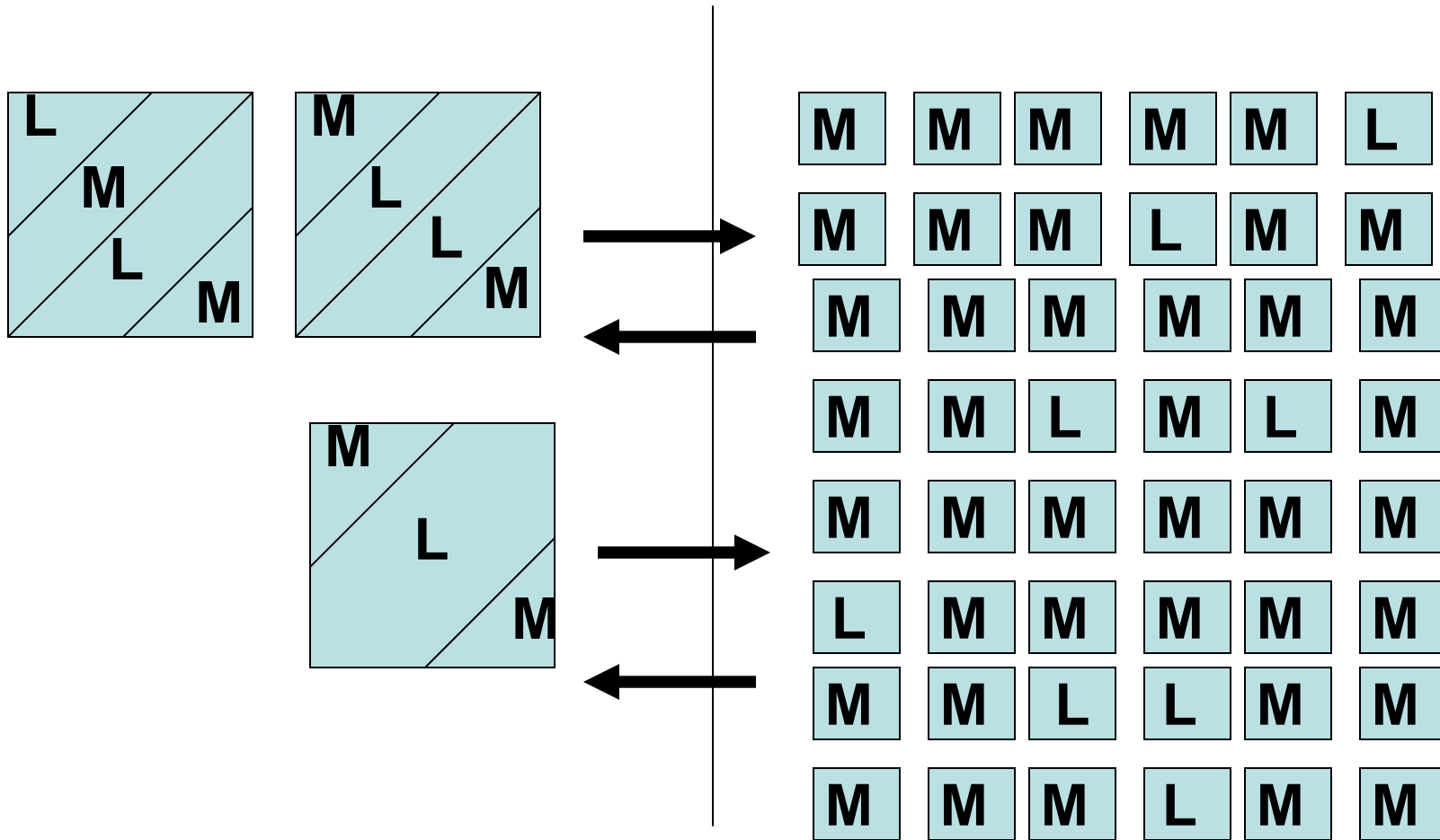
- **2 “treatments”**
  - **Mixed income redevelopments**
  - **Housing assistance vouchers**
- **2 kinds of people**
  - **Low income**
  - **Middle/high income**
- **initial conditions (low income developments, no vouchers, “natural” income mixing/segregation)**

# Baseline Pattern of Income Segregation



- **mixed income redevelopments**
  - **displacement of (some) low income residents**
  - **attraction of middle income residents**
  
- **vouchers**
  - **mobility from low income developments to mixed income neighborhoods**
  - **“flight” by (some) middle income residents**

# Income Segregation with Mixed Income Redevelopment and Vouchers



# Income Segregation with Mixed Income Redevelopment, Vouchers, and Homelessness

